Discrete vs continuous wavelet transform ppt

This section describes the major differences between the continuous wavelet transform (CWT) and the discrete wavelet transform (DWT) – both decimated and non-anaerated versions. cwt is a discrete version of CWT so that it can be implemented in a computational environment. This discussion focuses on the 1-D case, but is applicable to higher dimensions. The Cwt wavelet transform compares a signal with offset and scaled (stretched or shrunken) copies of a basic wave. If ψ(t) is a wavelet centered on t=0 with time support of [-T/2, T/2], then 1sin(t−us) is centered on t =u with time support [-sT/2+u, sT/2+u]. The Cwt function uses L1 normalization so that all frequency amplitudes are normalized to the same value. If 0 <> <1, the= wavelet= is= contracted= (shrunk)= and= if= s=>1, the wave is stretched. The mathematical term for this is dilation. See Continuous Wavelet Transform and Scale-Based Analysis for examples of how this operation extracts functions in the signal by matching it to dilated and translated wave races. The big difference between CWT and discrete wavelet transforms, such as dwt and modwt, is how the scale parameter is discretized. The CWT discretizes scale more nicely than the discrete wavelet transform. In CWT, you normally fix some bass which is a fractional power of two, such as 21/v where v is an integer greater than 1. The v parameter is often called the number of votes per octave. Different scales are obtained by increasing this base scale to positive integer forces, such as 2j/v j=1,2,3,.... The parameter for translation in the CWT disc disc discretized to integer values, denoted here by m. The resulting discrete wave races for CWT are the reason v is referred to as the number of votes per octave is because an increase in the scale by one octave (a doubling) requires v intermediate scales. For example, take 2v/v=2, and then increase the numerator in the exponent until you reach 4, the next octave. You move from 2v/v=2 to 22v/v=4. There are our intermediate steps. Common values for v are 10,12,14,16 and 32. The greater the value v is, the finer the discretization of the scale parameter, p. However, this also increases the required compute amount because CWT must be calculated for each scale. The difference between scales on a log2 scale is 1/v. See CWT-Based time-frequency analysis and continuous wavelet analysis of Modulated signals for examples of scale vectors with the CWT. In the discrete wavelet transform, the scale parameter is always discretized to integer forces of 2, 2j, j=1,2,3,..., so that the number of votes per octave is always 1. The difference between scales on a log2 scale is always 1 for discrete wavelet transformers. Note that this is a much coarser sampling of the scale parameter, s, than is the case with CWT. Furthermore, in the decimated (de-pardered) discrete wavelet transform (DWT), the parameter for translation is always proportional to the scale. This means that in scale, 2j, you</1,>translate with 2jm where m is a nonnegative integer. In nondecimated discrete wavelet transforms as modwt and swt, the scale parameter is limited to the powers of two, but the translation parameter is an integer as in CWT. The discrete wavelet for the DWT discrete wavelet takes after forms The nondecimated discrete wavelet transform discretized wavelet, such as the MODWT, is To summarize: the CWT and the discrete wavelet formers differ in how the discretize scale parameter. CWT typically uses exponential scales with a base smaller than 2, such as 21/12 . The discrete wavelet transform always uses exponential scales with the base equal to 2. Scales in the discrete wavelet form are the superiority of 2. Keep in mind that the physical interpretation of scales for both CWT and discrete wavelet transforms requires that the signal's sampling range be included if it is not equal to one. For example, suppose you're using CWT and you set your base to s0=21/12. To attach physical importance to that scale, you must multiply by the sampling interval Δt, so a scale vector covering approximately four octaves with the sampling interval taken into account is s0jΔt j=1,2,-48. Note that the sampling interval multiplies the scales, it is not in the exponent. For discrete wavelet transforms the base scale is always 2.The decimated and nondecimated discrete wavelet transforms differ in how they discretize the translation parameter. The decimated discrete wavelet transform (DWT), always translates with an integer multiple of the scale, 2jm. The nondecimated discrete wavelet transform translates through integer shifts. These differences in how scale and translation are discretized result in advantages and disadvantages for the two classes of wavelet transformers. These differences also determine use cases where a wave rotation transform is likely to produce superior results. Some important consequences of the discretization of the scale and translation parameter are: The DWT gives a sparse representation for many natural signals. In other words, the important features of many natural signals are captured by a subset of DWT coefficients that are usually much smaller than the original signal. This compresses the signal. With DWT, you always end up with the same number of coefficients as the original signal, but many of the coefficients can be close to zero in value. As a result, you can often throw away these coefficients and still maintain a high-quality signal approximation. With CWT, you go from N-samples for an N-length signal to an M-by-N matrix of coefficients of M equal to the number of scales. CWT is a very redundant transformation. There is significant overlap between wave races at each scale and between scales. The compute resources required to calculate CWT and store the coefficients are much larger than DWT. The non-decimated discrete wavelet transform is also superfluous but the redundancy factor is usually less than CWT, because the shell parameter is not discretized so nicely. For the non-decimated discrete wavelet transform, go from N samples to an L+1-by-N matrix of coefficients where L is the level of the transform. The strict discretization of scale and translation in DWT ensures that DWT is an orthopedic transform (when using an orthopedic wavelet). There are many advantages to orthonormal transformers in signal analysis. Many signal models consist of some deterministic signals plus white Gaussian noise. An orthonormal transformation takes this type of signal and outputs transform applied to the signal plus white noise. In other words, an orthonormal transform takes in white Gaussian noise and exits white Gaussian noise. The noise is unrelated at the entrance and exit. This is important in many statistical signal processing settings. In the case of DWT, the signal of interest is usually captured by some large large DWT coefficients, while the noise results in many small DWT coefficients that you can throw away. If you have studied linear algebra, you have undoubtedly learned many benefits of using orthonormal bases in the analysis and representation of vectors. The wavelets in DWT are like orthonormal vectors. Neither CWT nor the non-decimated discrete wavelet transformation are orthopedic transformers. The wavelets in the CWT and the nondecimated discrete wavelet transform are technically called, frameworks, they are linear-dependent sets. DWT is not shift-invariant. Since DWT downsamples, a shift in the input signal does not turn out as a simple corresponding shift in DWT coefficients at all levels. A simple shift in a signal can cause a significant realignment of signal energy in the DWT coefficients at scale. The CWT and nondecimated discrete wavelet transform are shift-invariant. There are some changes to DWT such as the dual-tree complex discrete wavelet transform that mitigates the lack of shift invariance in DWT, see Critical sample and oversampled Wavelet Filter Banker for some conceptual materials on this subject and Dual-Tree Complex Wavelet Transforms for an example. The discrete wavelet transformers are equivalent to discrete filter banks. Specifically, they are tree-structured discrete filter banks where the signal is first filtered by a lowpass and a highpass filter to provide lowpass and highpass subbands. Next, the lowpass subband is iteratively filtered by the same scheme to provide narrower octave-band lowpass and highpass subbands. In DWT, the filter outputs are sampled at each consecutive stage. In the non-decimated disk-pure wavelet transformation, the outputs are not sampled. The filters that define the discrete wavelet transforms typically have only a small number of coefficients so that the transformation can be implemented very efficiently. For both DWT and nondecimated discrete wavelet transform, you don't actually require an expression of wavelet. The filters are This is not the case with CWT. The most common implementation of CWT requires that you have wavelet explicitly defined. Although the non-decimated discrete wavelet transform does not downsample the signal, the filter bank implementation still allows for good computational performance, but not as good as DWT. The discrete wavelet transformer provides perfect reconstruction of the signal at inversion. This means that you can take the discrete wavelet transform of a signal and then use the coefficients to synthesize a precise representation of the signal to within numerical precision. You can implement an inverse CWT, but it is often the case that reconstruction is not perfect. Reconstructing a signal from the CWT coefficients is a much less stable numerical operation. The finer sampling of scales in CWT usually results in a signal analysis with higher fidelity. You can locate transients in your signal, or characterize oscillatory behavior better with CWT than with the discrete wavelet transformers. For further information on wavelet transformers and applications, see Based on the previous section, here are some basic guidelines for deciding whether to use a discrete or continuous wavelet transform. If your application is to obtain the sparsely possible signal representation for compression, denoising, or signal transmission, use DWT with wavedec. If your application requires an orthonormal transformation, use DWT with one of the ortatonal wave filter filters. The ortage al families in the Wavelet Toolbox™ are designated as type 1 wavelets in wavelet manager, wavemngr. Valid built-in ortactonal wavelet families are 'haar', 'dbN', 'fkN', 'coifN', or 'symN' where N is the number of vanishing moments for all families except 'fk'. For 'fk', N is the number of filter coefficients. See waveinfo for more details. If your application requires a shift-invariant transform but you still need perfect reconstruction and some measure of computational efficiency, try a nondecimated discrete wavelet transform like modwt or a dual-tree transform like dualtree. If your primary goal is a detailed time frequency analysis (scale) or precise location of signal transients, use CWT. For an example of time-frequency analysis with CWT, see CWT-Based Time-Frequency Analysis.For denoising a signal by threshold wavelet coefficients, use wdenoise function or Wavelet Signal Denoiser app. wdenoise and Wavelet Signal Denoiser provide default settings that can be applied to your data, as well as a simple interface to a variety of denoising methods. With the app you can visualize and denoise signals, and compare results. For examples of denoising a signal, see Denoise A Signal Using Standard Values and Denoise a Signal with Wavelet Signal Denoiser. For denoising images, use wdenoise2. For example, see Denoising Signals and Images.Om your application requires you to have a solid understanding of the statistical properties of the coefficients, use a discreet wave-race transform. There is an active effort to understand the statistical properties of CWT, but currently there are many more deployment results for the discrete wave stream transforms. The success of DWT in denoising depends largely on our understanding of its statistical properties. For an example of estimation and hypothesis testing that uses a nondecimated discrete wavelet transform, see Wavelet's analysis of financial data. Related examples more about about